

7. Cubes and Cube Roots

Opposite any number on D, read its cube on K. Thus Opposite 3.2 on D, read $3.2^3 = 3.28$ on K. The decimal point may be fixed by making a rough mental calculation.

Conversely, opposite a number on K, read its cube on D. Opposite 4.5 on K (left), read $\sqrt[3]{4.5} = 1.65$ on D. Opposite 45 on K (middle), read $\sqrt[3]{45} = 3.55$ on D. Opposite 450 on K (right), read $\sqrt[3]{450} = 7.64$ on D. Use left, middle or right third of K scale as shown in the following table.

a given number	left third of K	middle third of K	right third of K
	1~10 1000~10000 0.01~0.001 0.00001~0.000001	10~100 10000~100000 0.1~0.01 0.0001~0.00001	100~1000 100000~1000000 1~0.1 0.001~0.0001

8. Reciprocal

Opposite any number on C, read its reciprocal on CI. The number on CI is given by the red figures. Opposite 2.5 on C, read $\frac{1}{2.5} = 0.4$ on CI. Opposite 125 on C, read $\frac{1}{125} = 0.008$ on CI.

9. Another Fundamental Calculation

- a. $a^3b = x$ $1.5^3 \times 3.14 = 7.07$ Opposite 1.5 on D, set left index of C. Opposite 3.14 on B, read 7.07 on A.
- b. $a^3b^2 = x$ $72^3 \times 0.45^2 = 1050$ Opposite a on D, set right index of C. Opposite b on C, read x on A.
- c. $\frac{a}{d} = x$ $\frac{11^3}{4.9} = 24.7$ Opposite a on D, set b on B, Opposite index of C, read x on A.
- d. $\frac{a^3b}{c} = x$ $\frac{8.05^3 \times 0.34}{51.5} = 0.428$ Opposite a on D, set c on B. Opposite b on B, read x on A.
- e. $\sqrt{ab} = x$ $\sqrt{1.83 \times 0.26} = 0.69$ Opposite a on A, set index of B. Opposite b on B, read x on D.
- f. $\frac{a}{\sqrt{b}} = x$ $\frac{79.3}{\sqrt{2.35}} = 51.7$ Opposite a on D, set b on B. Opposite index of C, read x on D.
- g. $\frac{a\sqrt{b}}{c} = x$ $\frac{31.93 \times \sqrt{147}}{3.2} = 120.9$ Opposite a on D, set c on C. Opposite b on B, read x on D.
- h. $ad^3 = x$ $0.65 \times 2.3^3 = 7.91$ Opposite a on K, set index of C. Opposite b on C, read x on K.
- i. $\frac{ab^3}{c^3} = x$ $\frac{1.95 \times 6.08^3}{3.9^3} = 7.39$ Opposite a on K, set c on C. Opposite b on C, read x on K.
- j. $\sqrt{a^3b^3} = x$ $\sqrt{9.42^3 \times 4.12^3} = 242$ Opposite a on A, set index of B. Opposite b on B, read x on K. As a = 9.42, take a on left half of B, and as b = 4.12 take b on left half of B.

10. The Sine of an Angle

To get the sine of an angle a, we use S read at $0^\circ 45'$, set A or B and then use when S read at 6° , set scale C or D and then use. Opposite the mark at the right end of the back of the rule, set a on S. Opposite the index of D, read sine a on C.

Example $\sin 22^\circ$ Opposite the mark (back), set 22 on S. Opposite index of D, read sine $22^\circ = 0.375$ on C. If an angle is between $34'$ and $5^\circ 45'$, use S & T scale. In this range the sine of an angle is between 0.01 and 0.1. or Slide Rules with DI, you can read DI scale swing index on C.

11. The Cosine of an Angle

We find the cosine of an angle A by reading the sine of its compliment $90^\circ - A$, or $\cos 32^\circ = \sin(90^\circ - 32^\circ) = \sin 58^\circ$

12. The Tangent of an Angle

To get the tangent of an angle a, set a on T on the back face of the slide to the mark at the back right end of the rule, and read tan a on C against index of D.

Example $\tan 33^\circ$ Opposite the mark (back), set 33 on T. Opposite the index of D, read $\tan 33^\circ = 0.65$ on C.

13. Other Trigonometrical Functions

To get cotangent, secant and cosecant of an angle, we use the following formula.

$$\cot a = \frac{1}{\tan a} \quad \sec a = \frac{1}{\cos a} \quad \operatorname{cosec} a = \frac{1}{\sin a}$$

Thus, first take the tangent, cosine and sine of a then get their reciprocals.

14. Logarithms

Slide rules give only the mantissa or decimal part of the common logarithm of a number, and the characteristic or the integral part can be determined by inspection. We use in this calculation L and C (D) scale. In former case, we can directly read the mantissa of a number on L scale, but in later case, we operate as follows.

$\log 27.5 = 1.493$ Opposite 27.5 on D, set index of C. Opposite the mark line of the back face read 439 on L. Add characteristic 1, then the answer is 1.493

15. The LL scales

As mentioned previously, some of our slide rules have LL scales, which give the x^x and natural logarithms of numbers. We add some brief descriptions on LL_{1-4} scales.

a. e^{-x} ($0.01 < X < 10$)

These scales give the value e^x for values of x from 0.01 to 10. Opposite x on D, read e^x on LL_1 , LL_2 if x is between 0.01 and 0.1, LL_3 if x is between 0.1 and 1, LL_4 if x is between 1 and 10.

Example Opposite 3 on D, read $e^3 = 20.1$ on LL_3 ; $e^{0.3} = 1.350$ on LL_2 ; $e^{0.03} = 1.0304$ on LL_1 ;

b. Natural Logarithms

Logarithms to base e (2.71828) are called natural logarithms. We denote to natural logarithm of a number N by the symbol $\ln N$. We can read from LL scales natural logarithm of a number between 1.010 ($e^{0.01}$) and 22026 (e^{10}). Opposite 8.4 on LL_1 , read $\ln 8.4 = 2.13$ on D; Opposite 1.45 on LL_2 , read $\ln 1.45 = 0.372$ on D; Opposite 1.04 on LL_3 , read $\ln 1.04 = 0.0392$ on D;

16. The LL_{1-4} (or RLL) scales.

These scales operate with C or D in the same way that the LL_{1-4} scales combination operate with C and D.

a. e^{-x} ($0.001 < X < 10$)

Example If x is 3 Opposite $-x$ of set on D, $0.03 = 0.9704$ on LL_4 , $0.3 = 0.741$ on LL_3 , $3 = 0.497$ on LL_2 .

b. Natural Logarithms

Using LL_{1-4} , LL_{1-4} scales, we can read natural logarithm of a number between 0.999 and 0.00005. Example Opposite 0.04 on LL_4 read $\ln 0.04 = -3.2188$ on D; Opposite 0.65 on LL_3 read $\ln 0.65 = -0.431$ on D; Opposite 0.94 on LL_2 read $\ln 0.94 = -0.0619$ on D;

17. Calculation of X^y

Of course we can calculate the value of x^y by multiplying the common logarithm of x by y, and then reading the antilogarithm. More convenient method is as follows.

Example 1. $1.67^{4.5} = 2.102$ a. Opposite 1.67 on LL_2 , set index of C.

b. Opposite 1.45 on C, read 2.102 on LL_1 .

Example 2. $2.18^{4.5} = 37.1$ a. Opposite 2.18 on LL_3 , set index of C. b. Opposite 4.63 on C, read 37.1 on LL_1 .

Example 3. $0.64^{1.8} = 0.448$ a. Opposite 0.64 on LL_4 , set index of C. b. Opposite 1.8 on C, read 0.448 on LL_1 .